



| Instructions   | Example  |
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| <p>1. Carefully read the problem, note what numerical data is given, and what is being asked for.</p>  | <p>Find <b>two</b> numbers whose <b>sum is 60</b> and whose <b>difference is 14</b>.</p>   |
| <p>2. <b>Make a sketch, drawing, or picture of the described situation, and put all the given data from the problem on the drawing.</b> Look for what the problem's question is. In other words, what do they want to know? In this example, they want to know what the two numbers are.<br/> <b>Let <math>x</math> = one of the numbers, and let <math>y</math> = the other number.</b></p> | <p><i>Sum means <b>add</b>:</i></p> <p></p> <p><i>Difference means <b>subtract</b>:</i></p> <p></p> |
| <p>Write down any numerical relationships that the problem gives you. In this case, you need the sum and difference equations.</p>   | <p><b><math>X + Y = 60</math></b></p> <p><b><math>X - Y = 14</math></b></p>  |

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| <p>3. Look for other information (numbers, formula, etc.) that you can use to relate all the items.<br/>In this case, note that we have two equations and two unknowns, which may be solved by the substitution method.</p> | <ul style="list-style-type: none"> <li>• Take one equation and solve for <math>y</math> to get an expression containing <math>x</math>.</li> <li>• Next, substitute that expression for <math>y</math> in place of <math>y</math> in the other equation.</li> <li>• Then, you'll have one equation with a single unknown, <math>x</math>, in it.</li> <li>• Now you can solve for <math>x</math>.</li> </ul> |
| <p>4. Do the substitution method.</p>   | $X + Y = 60$ <p>Solving for <math>Y</math>,</p> $X + Y - X = 60 - X$ $Y = 60 - X$ <p>Substituting for <math>Y</math> in other equation,</p> $X - Y = 14$ $X - (60 - X) = 14$ $X - 60 + X = 14$ $2X - 60 + 60 = 14 + 60$ $2X = 74$ $X = 37$   |
| <p>5. <b>Solve for <math>y</math>:</b><br/>Go back to the first equation, and substitute for <math>x</math> to solve for <math>y</math>.</p>  | $Y = 60 - X$ <p>We just found <math>X</math> to be 37 so,</p> $Y = 60 - 37$ $Y = 23$   |
| <p><b>Check answers: 37 and 23.</b></p> <p>Is their sum 60? <math>37 + 23 = 60</math> ✓</p> <p>Is their difference 14? <math>37 - 23 = 14</math> ✓</p>  |  |